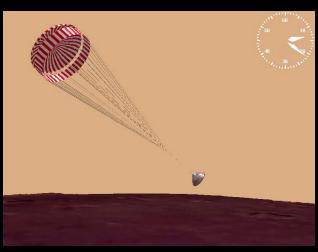
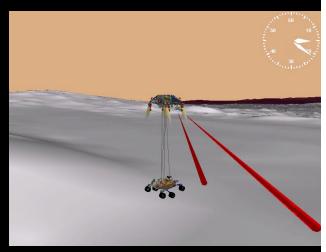
Flight Mechanics for Mission Scientists

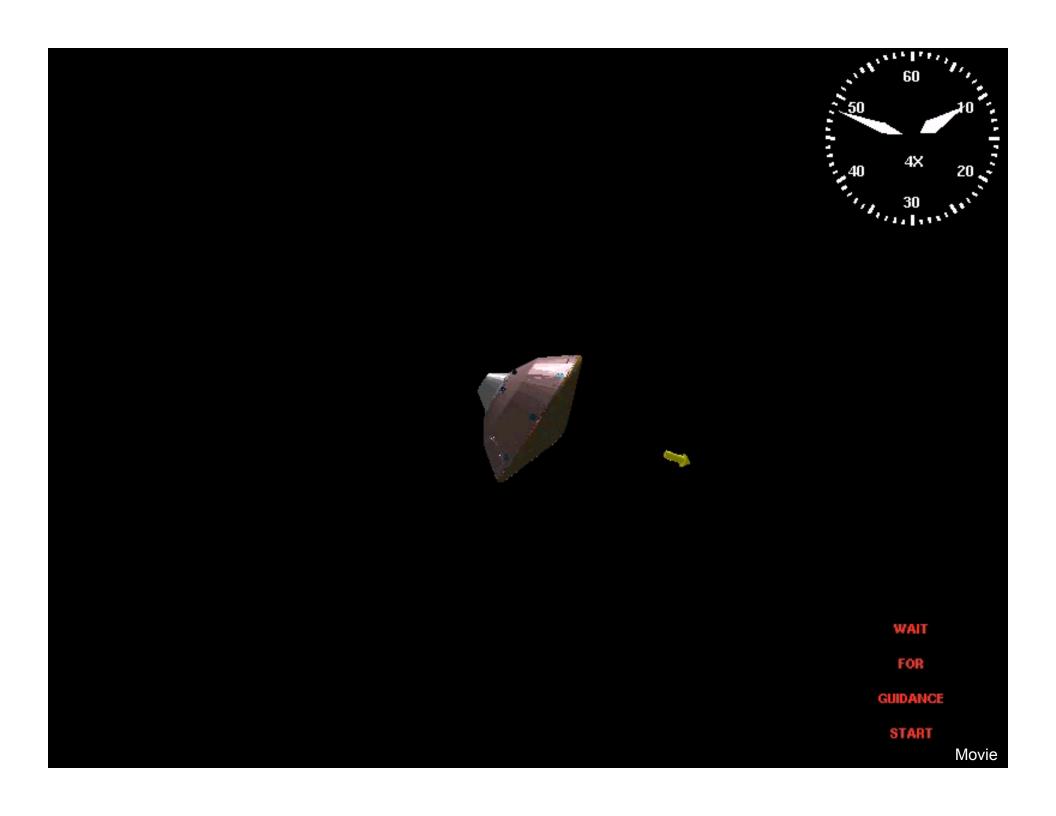


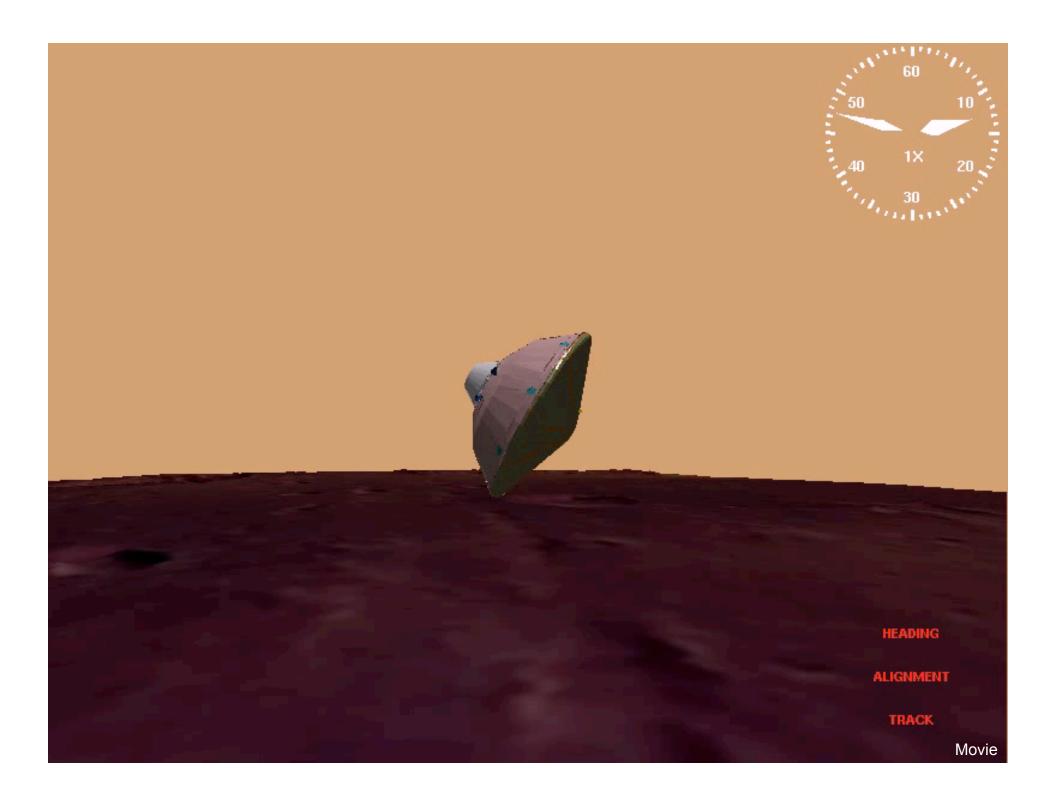


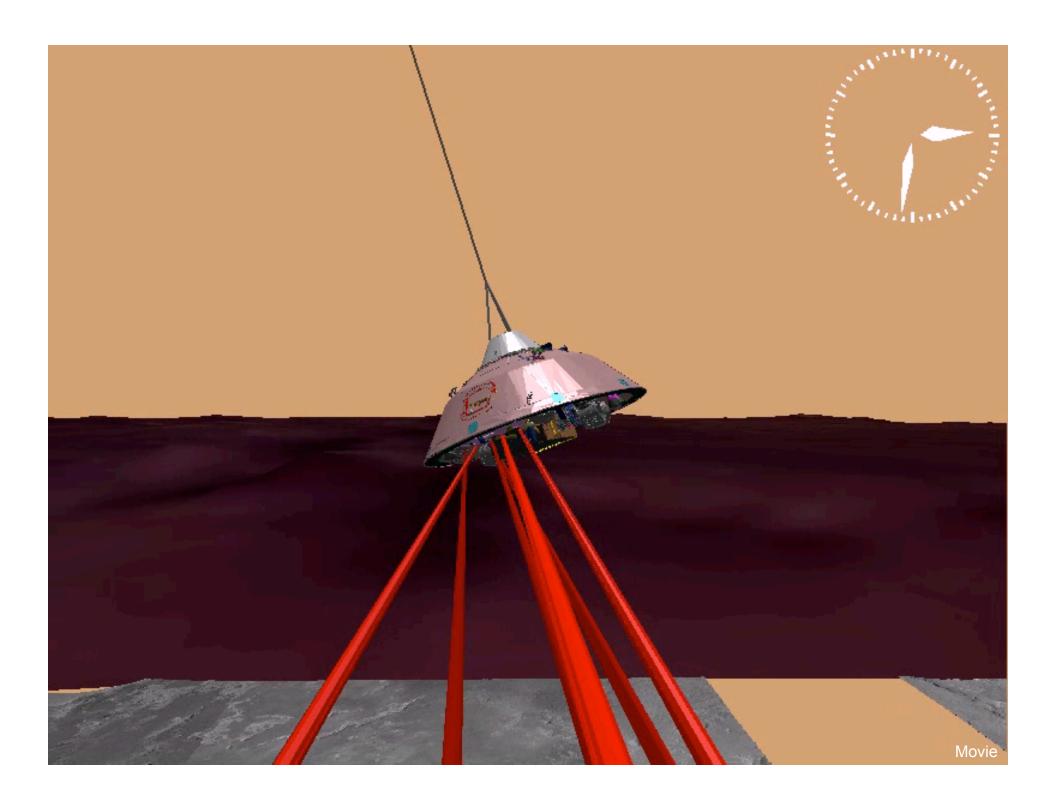


Juan R. Cruz
Atmospheric Flight and Entry Systems Branch
NASA Langley Research Center

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Flight Mechanics

Definition

The branch of engineering that studies the motion of aerospace vehicles in flight when acted upon by gravitational, aerodynamic, propulsive, and other external forces.

In this lecture I will focus on the flight mechanics of entry and descent vehicles, with an emphasis on:

- State variables, equations of motion
- Aerodynamics
- Improving communication between flight mechanics engineers and mission scientists

State Variables

<u>Twelve</u> state variables completely define the motion of the vehicle:

u, v, w - vehicle's center of mass velocity vector

p, q, r - vehicle's rotation rate vector

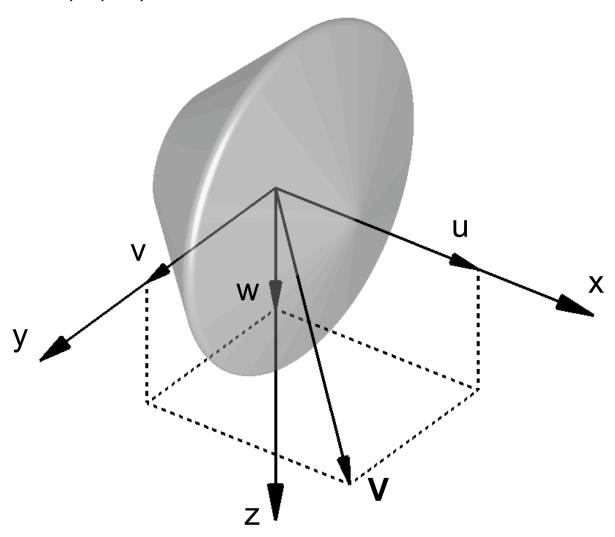
 ψ , θ , ϕ - vehicle's attitude; *Euler Angles*

 X_P, Y_P, Z_P vehicle's center of mass location vector

We will need one differential equation for each of these state variables

State Variables - Velocity

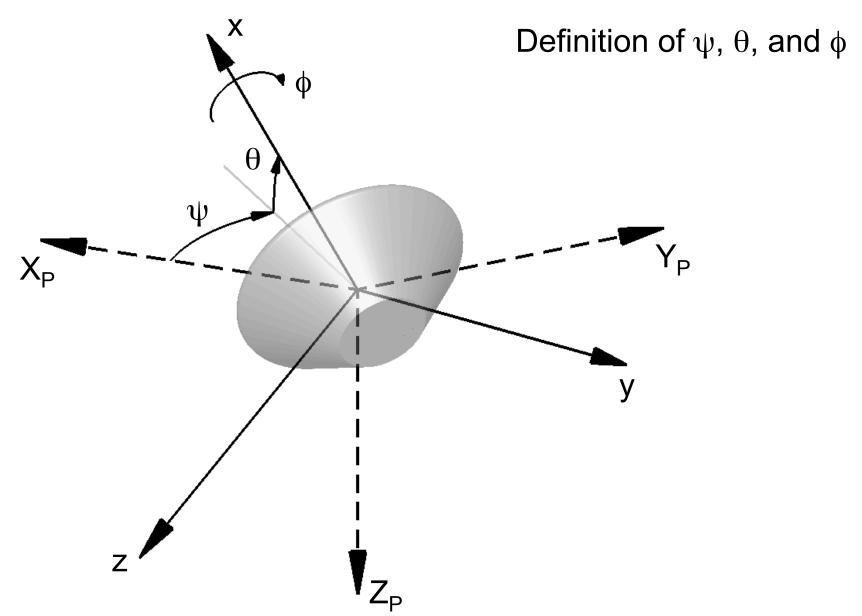
Definition of u, v, w, and V



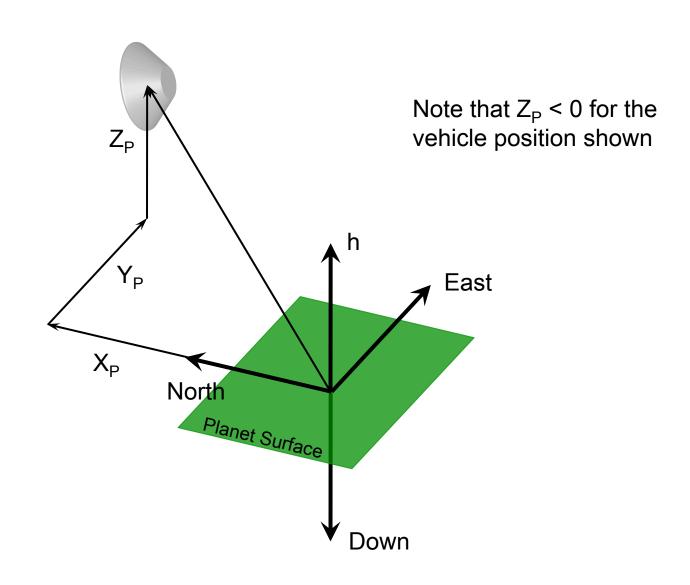
State Variables - Rotation

Definition of p, q, r, and Ω p, q, r, and Ω are shown by double arrow and arc arrow X

State Variables - Attitude



State Variables - Position



Equations of Motion

The equations of motion (EOM) can be written conceptually as:

$$\begin{bmatrix} m \end{bmatrix} \left\{ \dot{V} \right\} = \left\{ F_{gravity} + F_{propulsion} + F_{aero} \right\}$$
 These equations are coupled
$$\begin{bmatrix} I \end{bmatrix} \left\{ \dot{\Omega} \right\} = \left\{ M_{gravity} + M_{propulsion} + M_{aero} \right\}$$

$$\left\{\dot{\Theta}\right\} = \left\{\mathsf{f}_{\mathsf{Q}}\big(\Theta, \Omega\big)\right\}$$

$$\left\{\dot{X}\right\} = \left\{f_{X}\!\left(V,\Theta\right)\right\}$$

V - velocity

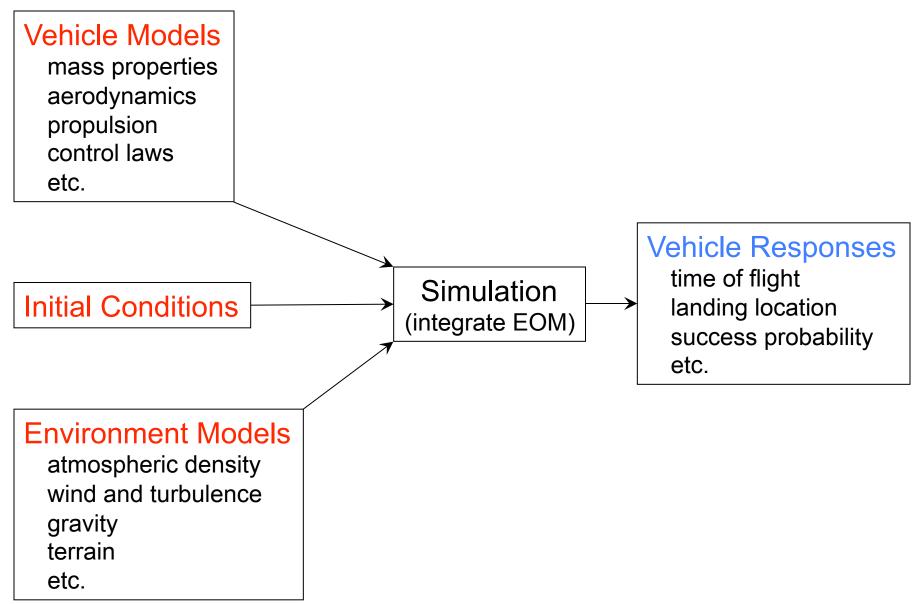
 Ω - rotation

 Θ - attitude

X - position

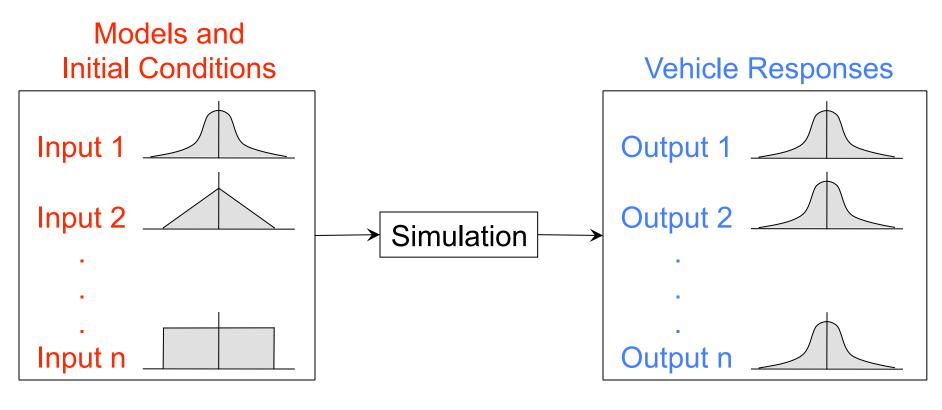
Standard numerical methods are used to integrate the EOM. Significant difficulties arise in obtaining accurate values for the aerodynamic forces and moments, F_{aero} and M_{aero} .

Modeling and Simulation



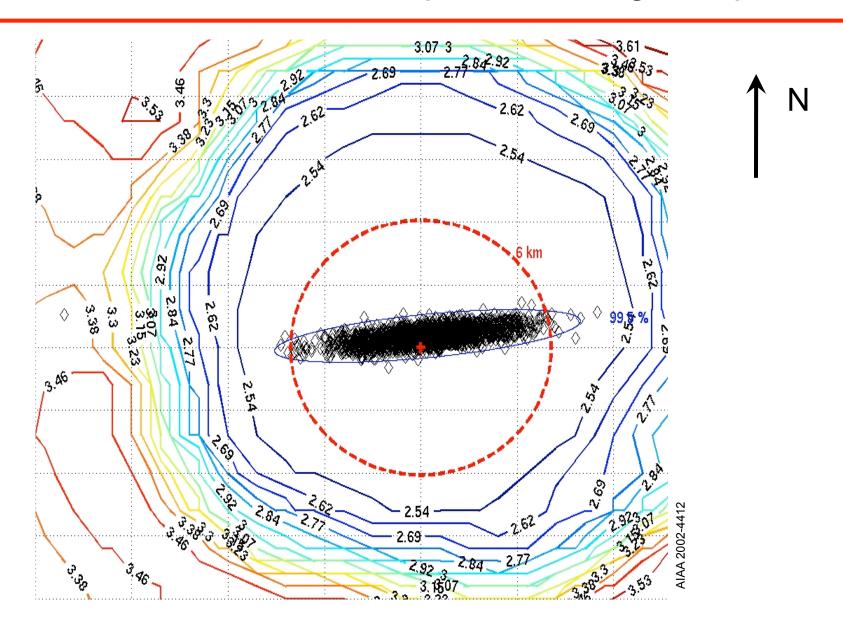
Uncertainty and Monte Carlo Simulation

Values for input quantities related to the vehicle models, initial conditions, and environment models are often only known in a statistical sense. The effect of the uncertainties in these quantities are addressed by executing the simulation 1000's of times using the Monte Carlo method.

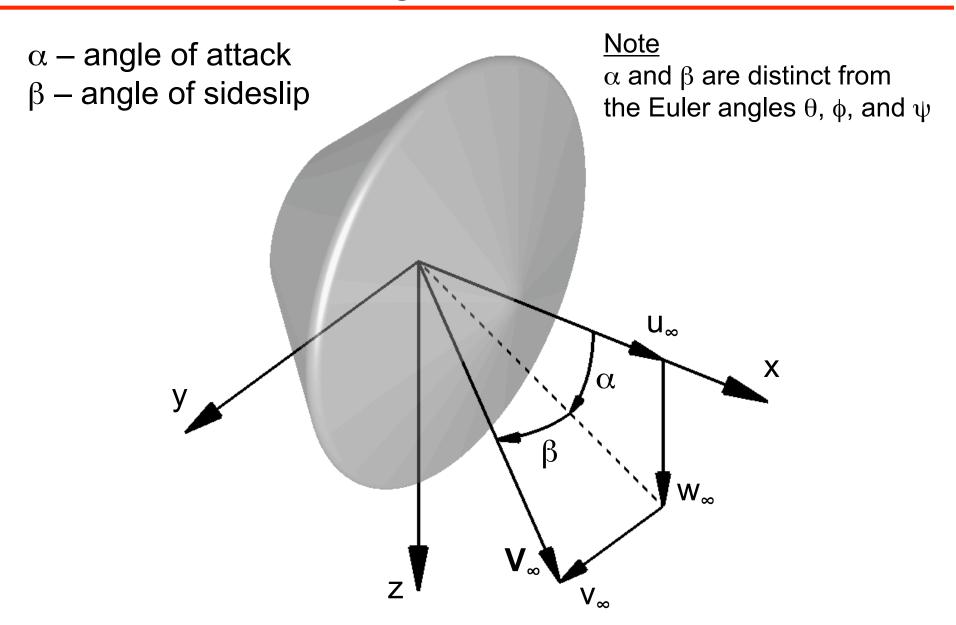


—— Calculate 1000's of trajectories ——>

Monte Carlo Simulation Example – Landing Footprint



Wind Relative Angles



Sources of Aerodynamic Data

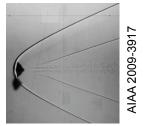
The needed aerodynamic data can be obtained in several ways:

Static Wind Tunnel Test



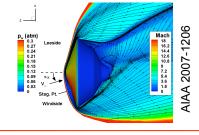


Dynamic Testing

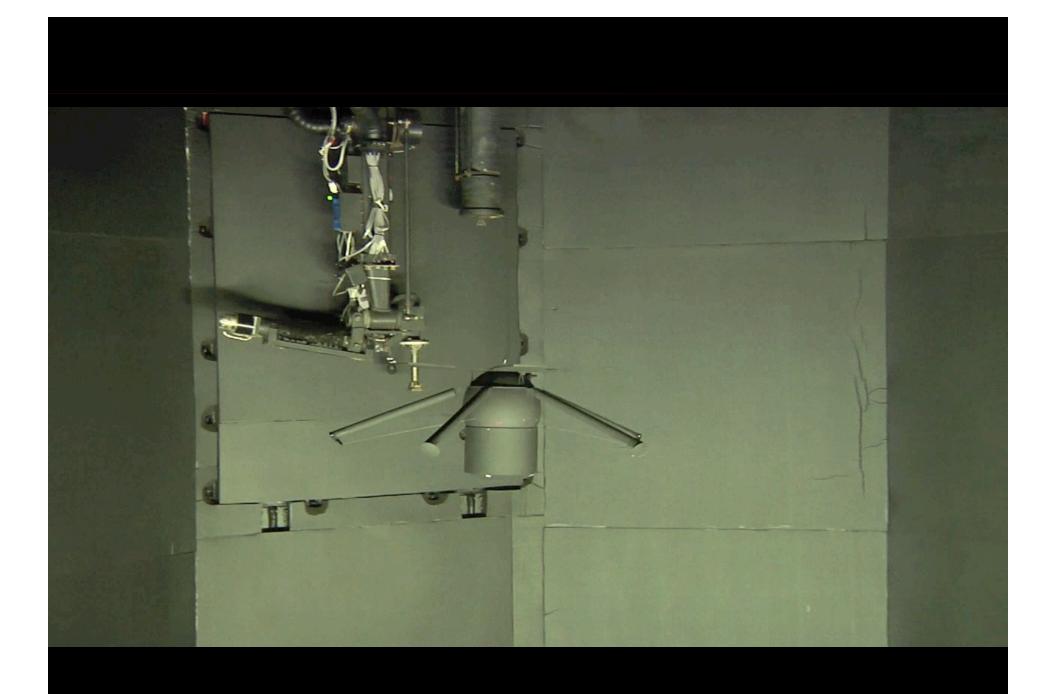




Computational Fluid Dynamics

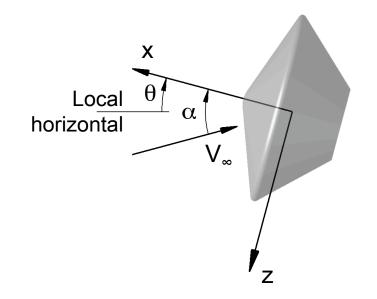


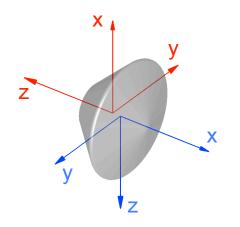
Regardless of the data source, aerodynamics model and data are often approximate and constitute a significant source of the uncertainty in flight mechanics simulations.



Terminology

- Be rigorous in the use of terminology
 - Example: angle of attack is generally not the same as the pitch angle; $\alpha \neq \theta$
- Be clear on the coordinate system being used
 - The standard body coordinate systems used in flight mechanics is often different than that used by the mechanical systems design team





Flight Mechanics: Blue Mechanical Systems: Red

Accuracy of Results

- Numerous assumptions are made in flight mechanics simulations. These assumptions affect the accuracy of the calculated responses.
 - Example: aerodynamic damping derivatives
- The accuracy of calculated responses varies between calculated responses
 - Example: dq/dt (rotational acceleration in pitch) is typically less accurate than q (rotational velocity in pitch)

Statistics

- Most of the input quantities and calculated responses are best characterized in terms of statistics
- Do not assume that the statistical distribution of calculated responses is normal (Gaussian) – often they are not!
 - Because of this, avoid specifying uncertainty in terms of the standard deviation, σ
 - Useful ways of describing the statistics of a response include Histograms and Cumulative Probability Graphs Mean, Median, and Percentiles

Requirements

- Requirements on calculated responses are best specified in statistical, not absolute terms
 - Example: X shall not exceed a value of Y at the 99.5 percentile level
- Be very specific in defining requirements related to calculated responses

Weak: The rotation rate shall be less than X rad/s

Better: The magnitude of the rotation rate vector, $|\Omega|$, shall be less than X rad/s 20 percent of the time from event A to event B.

Environments I

Environments are critical to accurate simulations

```
gravity field
atmospheric density
atmospheric speed of sound
wind
turbulence
```

 Some of these environment variables have first-order effects on the flight (e.g., atmospheric density)

Environments II

- Without some of these environment variables it is impossible to calculate certain responses
 - Example: wind and turbulence models are needed to calculate the flight dynamics of a vehicle in terminal descent
- The flight mechanics team will depend on the science team for definition of some or all of these environments